

CSc 461/561

Multimedia Systems

Lossy compression

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Compression

- Why compression
 - there is redundancy!
- How to compress
 - remove data/information redundancy
- Lossless compression
- Lossy compression
 - remove information redundancy *adequately*
 - information loss, but higher compression ratio!

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Lossy compression examples

- Why lossy compression is possible?

- some information is more important than others for *human*
- keep the important one



Original



Compression Ratio: 7.7
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Compression Ratio: 12.3
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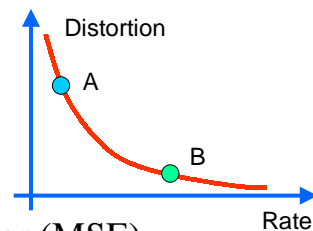


Compression Ratio: 33.9

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Tradeoff: rate vs distortion

- Rate
 - # of bits per source symbol
- Distortion
 - one measure: mean square error (MSE)
 - x : original value; y : reconstructed value
 - $MSE = [(x_1 - y_1)^2 + (x_2 - y_2)^2 + \dots + (x_N - y_N)^2] / N$
- Rate vs distortion
 - lower rate, higher distortion



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Quantization

- Quantization (recall audio A/D)
 - use a discrete value to represent a value range
 - information loss!
- The smaller range, the less distortion
 - granular distortion
- Quantization steps
 - uniform: all ranges have the same size
 - non-uniform: otherwise

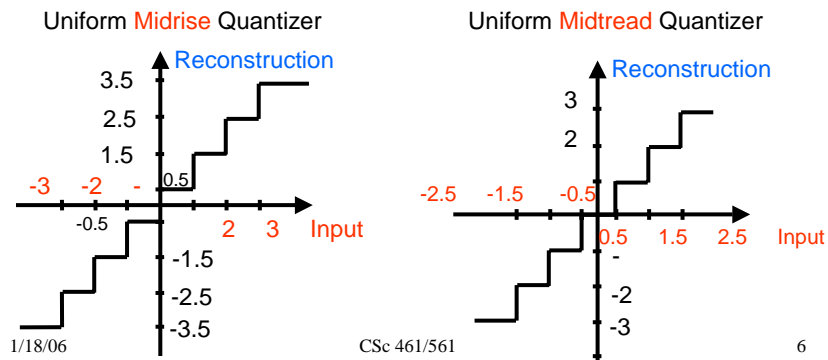
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Uniform quantization

- Quantization step: uniform
- Two constructions: midrise, midtread



Signal-to-quantization-noise ratio

- Quantization
 - n bits; 2^n steps for $[-X_{\max}, X_{\max}]$
 - step size: $\Delta = 2X_{\max} / 2^n$
 - granular distortion: $\sigma_q^2 = \int_{-\Delta/2}^{\Delta/2} (x-0)^2 \frac{1}{\Delta} dx = \frac{1}{12} \Delta^2$
- SQNR in dB
 - $10 \log_{10} \text{signal_energy} / \text{noise_energy}$
 - $= 10 \log_{10} [(2X_{\max})^2/12] / [\Delta^2/12] = 20n \log_{10} 2$
- One more bit adds 6 dB to SQNR

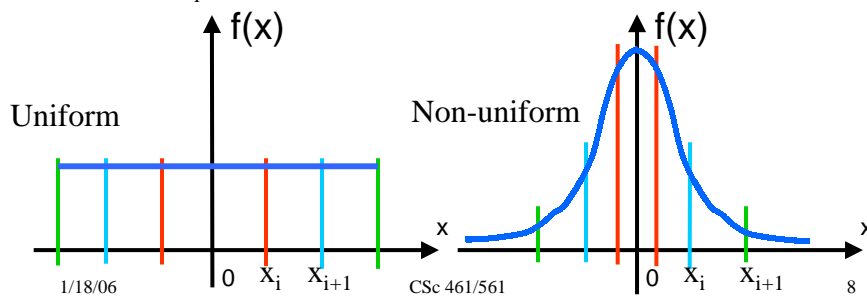
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Non-uniform quantization

- Recall u-law or A-law voice compander
- How to choose quantization steps?
 - $\int_{x_i}^{x_{i+1}} f(x) dx = 1/2^n$



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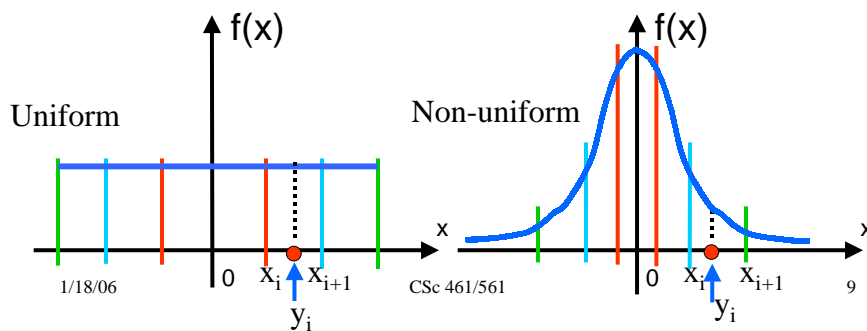
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Non-uniform quantization: more

- How to represent a range?

- $\int_{x_i}^{x_{i+1}} f(x) dx = 1/2^{n+1}$

- when uniform: $y_i = (x_i + x_{i+1})/2$



Transformation

- Transformation
 - represent information in another space
 - identify and remove (hard-to-remove) correlation, i.e., redundancy, in the original space
 - information loss!
 - e.g., time/space \Rightarrow frequency (FFT)
- Inverse transformation
 - represent the info back in the original space

Discrete Cosine Transform

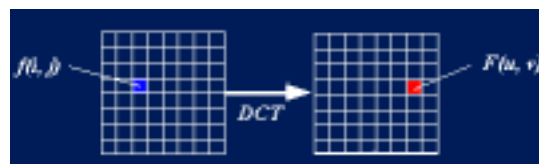
- Recall: a wave is of many *waves*
- “Any signal can be expressed as a sum of multiple signals that are sine or cosine waveforms at various amplitudes and frequencies.”
- Cosine transform: using cosine waveforms
- DCT: integer indexes
 - widely used in image compression (e.g., JPEG)

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DCT: more



- 2-D DCT (8x8); $C(x)=1/\sqrt{2}$ when $x=0$

$$F(u, v) = \frac{1}{4} C(u)C(v) \left[\sum_{i=0}^7 \sum_{j=0}^7 f(i, j) \cos \frac{(2i+1)u\pi}{16} \cos \frac{(2j+1)v\pi}{16} \right]$$

- Inverse 2-D DCT (IDCT); $C(x)=1$ otherwise

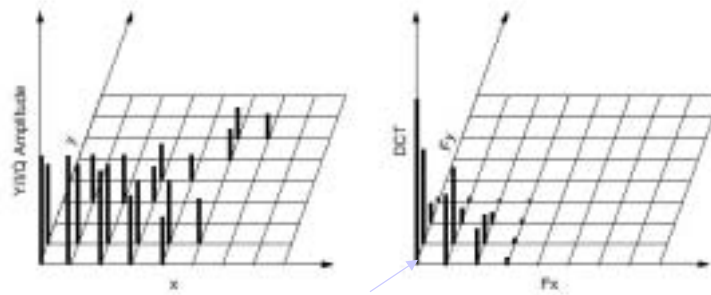
$$f(i, j) = \frac{1}{4} C(u)C(v) \left[\sum_{u=0}^7 \sum_{v=0}^7 F(u, v) \cos \frac{(2i+1)u\pi}{16} \cos \frac{(2j+1)v\pi}{16} \right]$$

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DCT: examples



Original values of an 8x8 block
(in spatial domain)

Corresponding DCT coefficients
(in frequency domain)

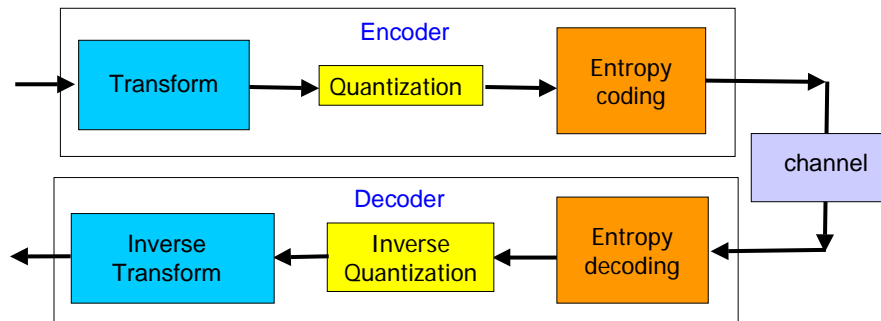
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Lossy + lossless compression

- In a big picture...



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This lecture

- **Multimedia manipulation**
 - lossy compression
 - rate vs distortion
 - quantization: uniform vs non-uniform
 - transformation: DCT
- **Explore further**
 - wavelet-based coding [Ref: Li&Drew 8.6.1]

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Next lecture

- **Multimedia manipulation**
 - audio compression [Ref: Li&Drew Chap 13-14]
 - quick review on PCM, DPCM and ADPCM
 - examples: MPEG audio [14.1-2]

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