Preferential Infinitesimals for Information Retrieval

Maria Chowdhury, Alex Thomo and William Wadge University of Victoria, Canada

Searching



Texts Search - Microsoft Internet Explorer	×
File Edit View Favorites Tools Help	7
🚱 Back 🔹 🛞 👻 📓 🏠 🔎 Search 👷 Favorites 🤣 🔗 + 🌺 🔯 🔹 💭 🧐 🆓	
Address 🗃 http://internetshakespeare.uvic.ca/Library/Texts/search/	
INTERNET SHAKESPEARE EDITIONS ome Plays & Poems Life & Times Performance Resources Search Site Map About Discussion Links	
The Foyer. The Kibrary. The Theater. The Annex. Search refinements Speaker: Near this text: Search Search	
Please enter some search text.	
Top of Page Policy on Quality Content Policy on Copyright How to cite this page	
This site is supported by the University of Victoria and the Social Sciences and Humanities Research Council of Canada.	
	<u>~</u>
alle and a second secon	



(No) Ranking ...



(No) Ranking ...

Well, do not then. For since you loue me not, I will not loue my selfe. Do you not loue me? Nay, tell me if thou speak'st in iest, or no.

Henry the Fourth, Part One (Folio) Line 942 Go to Act 2, Scene 3 / Go to Page 8

This hit with three occurrences of "loue" appears 10th in the list.

IR Ranking

- Term frequency (TF)
- Inverse document frequency (IDF)
- TF-IDF weighting Scheme

Term frequency (TF)

Normalized term frequency of t_i in d_j is

$$tf_{ij} = \frac{f_{ij}}{\max\{f_{1j}, \dots, f_{mj}\}}$$

maximum is computed over the terms that appear in document d_i

Inverse document frequency (IDF)

Inverse document frequency of term t_i is

$$idf_i = \log \frac{n}{n_i}$$

TF×IDF weighting scheme

TF×IDF weighting scheme assigns to term t_i a weight in document d_i given by

$$tf - idf_{ij} = tf_{ij} \times idf_i$$

- Then each document is represented as a vector of tf-idf values.
- A query, e.g. loue, woman, is also represented as vector.
- Document-query similarities are computed using cosine similarity.

loue+woman	match all 💉
match all 👻 character speeches 👻	
	Ioue+woman match all v character speeches v

Found 42 hits in 2.610999999999998 seconds.

Hits 1 to 25 of 42

Next

And when I am a horsebacke, I will sweare I loue thee infinitely. But hearke you *Kate*, I must not haue you henceforth, question me, Whether I go: nor reason whereabout. Whether I must, I must: and to conclude, This Euening must I leaue thee, gentle *Kate*.

50

- Whether I must, I must: and to conclude, This Euening must I leaue thee, gentle *Kate*. I know you wise, but yet no further wise Then *Harry Percies* wife. Constant you are, But yet a woman: and for secrecie,
- ⁵⁵ No Lady closer. For I will beleeue Thou wilt not vtter what thou do'st not know, And so farre wilt I trust thee, gentle Kate.

Henry the Fourth, Part One (Folio) Line 946 Go to Act 2, Scene 3 / Go to Page 8

Text to find:	loue+Juliet	match all 💌
Search in:	match all 💙 character speeches 💙	
Coarab rafinamenta		
Speaker:		
Near this text:		

Found 46 hits in 2.002 seconds.

Hits 1 to 25 of 46

Next

Iul. My onely Loue sprung from my onely hate,

Too early seene, vnknowne, and knowne too late, Prodigious birth of Loue it is to me, That I must loue a loathed Enemie.

Denie thy Father and refuse thy name: Or if thou wilt not, be but sworne my Loue,

³⁰ And Ile no longer be a *Capulet*.

Romeo and Juliet (Folio) Line 721 Go to Act 1, Scene 5 / Go to Page 6

Romeo and Juliet (Folio) Line 722 Go to Act 1, Scene 5 / Go to Page 6

Romeo and Juliet (Folio) Line 828 Go to Act 2, Scene 2 / Go to Page 7

Preferences

loue &woman

Semantics:

- Rank documents w.r.t. "loue" first.
- Among documents ranked equally w.r.t. "loue" those with more occurrences of "woman" should be ranked higher.
- Don't ignore documents with "loue" occurrences, but without "woman" occurrences.



- Suppose a user wants to retrieve documents about "image-information-retrieval" and among those, he would be interested in documents mentioning "google-search" and "google-ranking".
- What would happen if the user gives the following query:

image-information-retrieval, google-search, googleranking



e





music-information-retrieval:100, google-search, googleranking

- "100 times more important" seems quite convincing in colloquial talking!
- However, what if, according to Google, documents about google-search were 1000 times more important than documents about music-informationretrieval?

Infinitesimals

 \mathbf{z} is said to be infinitely small or infinitesimal iff $-a < \varepsilon < a$ for every $a \in \mathbb{R}^+$. Ref. Jerome Keisler. Infinitesimal Calculus. For a, b, r, $s \in \mathbb{R}^+$, we have • $a\varepsilon^r < b\varepsilon^s$ iff r > s• $a\varepsilon^r < b\varepsilon^r$ iff a < b. Examples ■ 10 ε² < ε</p> ■ 1,000,000 ε² < ε $5\epsilon + 7\epsilon^2 + 3\epsilon^3 < 6\epsilon + 100\epsilon^2$



music-information-retrieval, google-search:ε, googleranking:ε².

Or say...

music-information-retrieval, google-search:2ε, googleranking:ε.

Document structure

paper \rightarrow preamble body preamble \rightarrow title author+ abstract keywords body \rightarrow introduction section* related-work? References

Document structure with weights

paper \rightarrow (preamble:3) (body:1)

- preamble \rightarrow (title:2) (author:1)+ (abstract:1) (keywords:10)
- body \rightarrow (introduction:2) (section:1)* (related-work: ϵ)? (references: ϵ^2)

Normalizing weights

- Since an annotated element can be nested inside other elements, which can be annotated as well, the question is: How to compute the actual weight of an element in a DTD?
- Multiply weights along ancestor path?
 - What we want is "an element to never be more important than its parent."

Normalizing weights

paper \rightarrow (preamble : 1) (body : 1/3)

preamble \rightarrow (title : 1/5) (author : 1/10)+ (abstract : 1/10) (keywords : 1)

body \rightarrow (introduction : 1) (section : 1/2)* (related-work : $\varepsilon/2$)? (references : $\varepsilon^2/2$)

TF revisited

Suppose that term t_i occurs f_{ijk} times in element e_k of document d_i

$$tf_{ij} = \frac{\sum_k w_k f_{ijk}}{\max\{\sum_k w_k f_{1jk}, \dots, \sum_k w_k f_{mjk}\}}$$

TF revisited – Example

- Suppose that t_i occurs
 - once in the keywords element,
 - twice in the abstract element,
 - three times in the section elements,
 - four times in the related-work element, and
 - twice in the references element
 - of document d_{i} .

Then, the numerator of the tf_{ij} fraction will be $1 \cdot 1 \cdot 1 + 1 \cdot (1/10) \cdot 2 + (1/3) \cdot (1/2) \cdot 3 + (1/3) \cdot (\varepsilon/2) \cdot 4 + (1/3) \cdot (\varepsilon^2/2) \cdot 2 = 1.7 + (2/3) \cdot \varepsilon + (1/3) \cdot \varepsilon^2$.

IDF revisited

- For an element-weight pair (e_h, w_h) , let
 - *n^h* be the total number of such elements in the XML documents in collection.
- Suppose that a term t_i occurs in n_{hi} of them.
 - Then, we define the IDF of t_i wrt these elements as

$$idf_{hi} = \log \frac{n_h}{n_{hi}}$$

IDF revisited

Next, we define the IDF score of a term t_i with respect to the whole document collection as

$$idf_i = \frac{\sum_h w_h \cdot idf_{hi}}{\sum_h w_h}$$

TF×IDF weighting scheme

TF×IDF weighting scheme assigns to term t_i a weight in document d_i given by

$$tf - idf_{ij} = tf_{ij} \times idf_i$$

- Then each document is represented as a vector of tf-idf values.
- A query, is also represented as vector.
 - The values are exactly those hyperreal numbers specified by the user multiplied by the IDF scores of the terms.

Documents and queries

We rank the documents by computing their similarly score with respect to a query q.

$$cosine(\mathbf{w}_j, \mathbf{w}_q) = \frac{\langle \mathbf{w}_j, \mathbf{w}_q \rangle}{||\mathbf{w}_j|| \times ||\mathbf{w}_q||} = \frac{\sum_{i=1}^m w_{ij} \times w_{iq}}{\sqrt{\sum_{i=1}^m w_{ij}^2} \times \sqrt{\sum_{i=1}^m w_{iq}^2}}$$

Experiments

- Corpus I: On-line Internet Shakespeare Edition of the English Department, University of Victoria
 33,000 speeches.
- Corpus II: An INEX (INitiative for the Evaluation of XML retrieval) corpus.
 - Numerous XML documents of moderate size.
 - Topics of documents vary from climate change to space exploration.
 - We preferentially annotated the DTD of this collection.
- Representative queries given in the full version:
 - http://www.cs.uvic.ca/~thomo/publications/aiai09.pdf

Example

Q: Norway climate: ε information: ε^2 ,

Our System:

<title>Climate in Norway< /title>

<description>Find information about the climate in
Norway in summer./description>

<narrative>I would like to travel to Norway in July, but I have no idea about the weather. I don't know which clothes to put in my bag. To be relevant, a paragraph or a document should let me know the mean average temperature in this season and the precipitation level, or just give me an information like continental climate or polar climate...

< /narrative>

Example

Q: Norway climate: ε information: ε^2 ,

Classical System:

<title>Ontology< /title>

<description>Find information about ontology.</description>

<narrative>An ontology is typically a hierarchical data structure containing all the relevant entities and their relationships and rules within that domain (e.g., a domain ontology). ...For it plays a very important role in **information** extraction, entity recognition etc., I would like to learn more **information** about the introduction of it and how it works. Besides, I expect to find relevant **information** as elements in larger documents ...

< /narrative>

Thank you!

References

Maria Chowdhury, Alex Thomo, William W. Wadge. Preferential Infinitesimals for Information Retrieval. AIAI 2009: 113-125

Maryam Khezrzadeh, Alex Thomo, William W. Wadge. Harnessing the power of "favorites" lists for recommendation systems. RecSys 2009: 289-292