

Write down the definition of Big Oh.

Use it to prove that:

1.  $T(n) = 6n^4 - 60n^2 + 7$  is in  $O(n^4)$ .

2.  $T(n) = 2^0 + 2^1 + 2^2 + \dots + 2^n$  is in  $O(2^n)$ .



# SCRATCH

**Teach kids in  
grades 6-9 to code!**

**Winners will be  
PAID to develop  
games that we'll  
host on [csc.uvic.ca](http://csc.uvic.ca)**

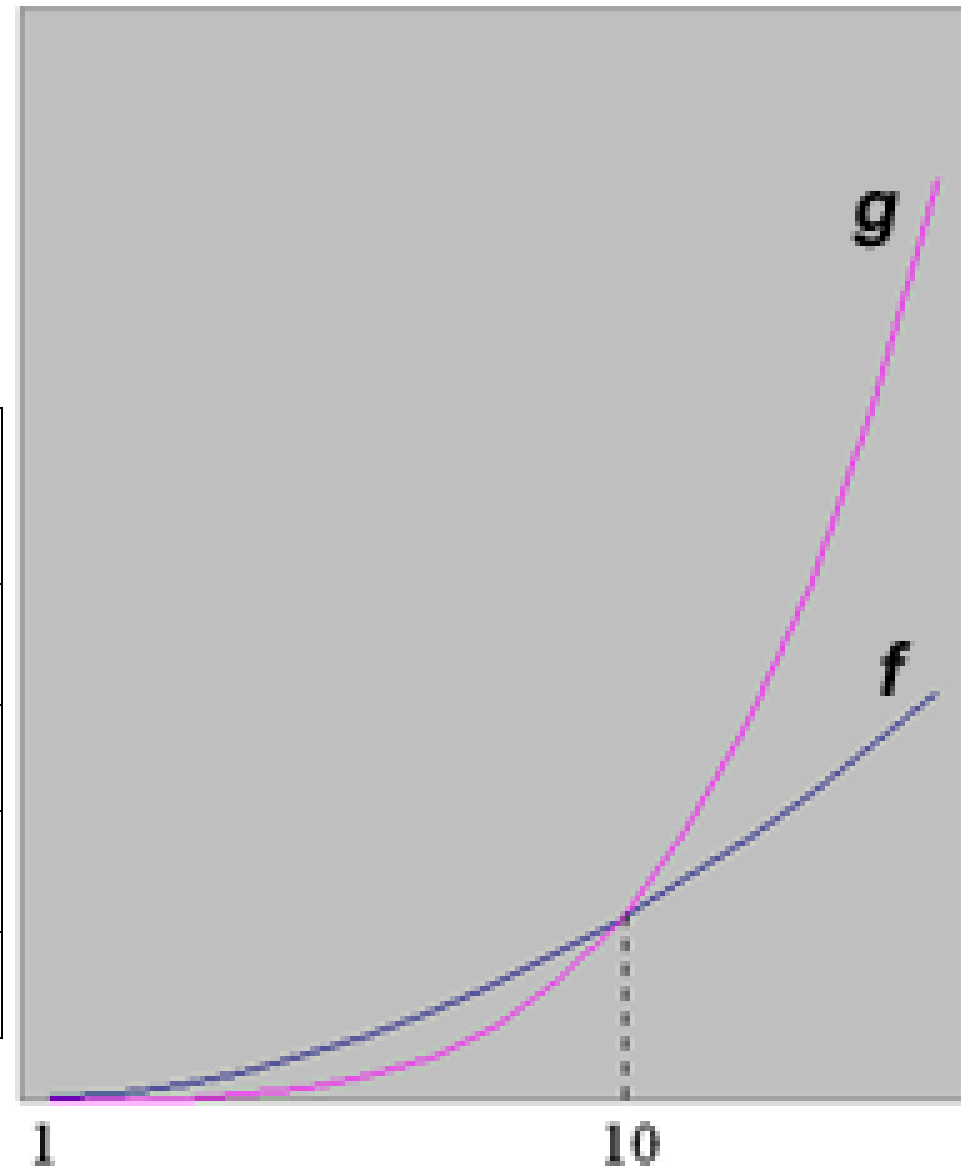


**PITCH YOUR SCRATCH PROJECT IDEA  
FRIDAY SEPTEMBER 27 at 2:30 IN ECS 660**

$$f(n) = 100 n^2$$

$$g(n) = n^4$$

$n$	$f(n)$	$g(n)$
10	10,000	10,000
50	250,000	6,250,000
100	1,000,000	100,000,000
150	2,250,000	506,250,000



Example from:

<http://www.cs.odu.edu/~toida/nerzic/content/function/growth.html>

Assume that  $T, f$  are functions mapping the natural numbers  $\{0, 1, 2, 3, \dots\}$  into the reals.

**Definition: "Big Oh"** A function  $T(n)$  is in  $O(f(n))$  if there exist constants  $n_0 \geq 0$ , and  $c > 0$ , such that for all  $n \geq n_0$ ,  $T(n) \leq c * f(n)$ .

Important: here I differ from older usage in defining  $O(f(n))$  to be a *set* of functions. This will prove useful later.

Big-Oh	Informal name
$O(1)$	constant
$O(\log n)$	logarithmic
$O(n)$	linear
$O(n \log n)$	$n \log n$
$O(n^2)$	quadratic
$O(n^3)$	cubic
$O(2^n)$	exponential
$O(n^c)$ for constant $c$ ,	polynomial time

Assume that  $T$ ,  $f$  and  $g$  are functions mapping the natural numbers  $\{0, 1, 2, 3, \dots\}$  into the reals.

**Definition: "Omega"** A function  $T(n)$  is in  $\Omega(f(n))$  if there exist constants  $n_0 \geq 0$ , and  $c > 0$ , such that for all  $n \geq n_0$ ,  $T(n) \geq c * f(n)$ .

**Definition: "Theta"** The set  $\Theta(g(n))$  of functions consists of  $\Omega(g(n)) \cap O(g(n))$ .

## Regular Office hours:

**Monday:** no office hours.

**TWF:** 12:30-1:30

**TWF:** either 1:30-2:30 if I have no meeting scheduled, or 2:30-3:30 otherwise. The slots for the week will be announced in class or you can ask me by e-mail.

**Thursdays:** by appointment for students who have classes during the other office hours.

# Announcements

Office hours this week:

T 12:30, 2:30

W 12:30, 1:30

F 12:30, 1:30

Please let me know  
if you plan to  
attend at one of  
these.



Assignment #2 parts A (due Fri. Oct. 4) and B (due Tues. Oct. 8) are posted. Read through them and let me know if you have any questions.

Relevant sections of text:

1.1: Java review.

1.2-1.3: Programming basics review.

1.4: Algorithm analysis.

We will cover 1.5 later when we do graph algorithms.

Now: Ch. 2: Sorting.

For recurrences/induction: Use a Math 122 text.

For the rest of this lecture, we covered the time complexity of mergesort.